

An Information Flow-Based Sea Surface Height Reconstruction Through Machine Learning

Yineng Rong¹ and X. San Liang¹

Abstract—The advent of satellite altimetry datasets of sea surface height (SSH) is a major advance in oceanography and other Earth system sciences. However, while the along-track data coverage is dense, the relatively poor resolution between tracks poses a challenge to the reconstruction of those processes such as mesoscale and submesoscale eddies. This study proposes a machine learning algorithm based on a causal inference tool, i.e., the Liang–Kleeman information flow (L-K IF) analysis, to address the challenge. For a region in the South China Sea where eddies frequently appear but unobserved, it is shown that the algorithm can reconstruct the desired mesoscale eddies in a remarkably successful way in geometry, orientation, strength, etc., while with the objective analysis interpolation or the traditional neural network technique, the results are not satisfactory. This study provides prospects for developing the next generation of SSH products with the available altimetry data.

Index Terms—Causal inference, Liang–Kleeman information flow (L-K IF), machine learning, sea surface height (SSH).

I. INTRODUCTION

PERHAPS, one of the most significant achievements in satellite observation is the successful global reconstruction of a spatiotemporal field of sea surface height (SSH), an important ocean variable that allows for an accurate estimation of *in situ* large-scale ocean circulation (see [1] for a review). This not just sets a milestone in oceanography but also aids to advance atmospheric and other Earth sciences in the fields of, say, Madden–Julian oscillation (see [2]), El Niño–Southern Oscillation (ENSO) (see [3]–[6]), Indian Ocean Dipole (IOD) (see [7], [8]), and global change (see [9]–[11]), to name but a few. Indeed, during the past 30 years, satellite altimeters have gradually become a major observing technique in geoscience due to their dense resolution in space and time, as well as the simultaneous coverage on a global scale. For example, Fig. 1 shows the track of the Jason-2 satellite altimeters over the South China Sea. The along-track SSH can

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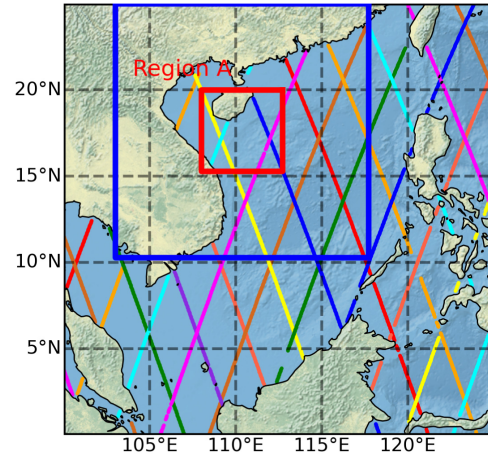


Fig. 1. Scatter of the Jason-2 trajectory over the South China Sea from January 1 to January 10, 2011. Different colors represent the trajectories on different days. The red box between Hainan Island and Vietnam is region A as referred to in the text; the blue one is the observation region for region A.

resolve waves with a wavelength as small as 30–50 km, with a root-mean-square error (RMSE) of only 2 cm.

With the densely covered data along the track, the resolution between the tracks, however, is in general not satisfactory. As a result, the global mesoscale resolution is rather limited, mainly due to the spatial and temporal gaps between the altimeter-derived SSH profiles. Currently, the mapping of the SSH observations onto the 2-D grid is mainly through the widely adopted global suboptimal space–time objective analysis (OA) [12] together with optimal interpolation (OI) (see [13]–[15]). The spatial gap can be reduced by using the multisatellite altimeter data [15]–[18], and the temporal resolution can be improved with dynamic interpolation (DI) [19]. Nonetheless, so far as of today, mesoscale and synoptic variabilities of SSH are still poorly reconstructed [20].

The widely used OA method employs a statistical estimation under a linear assumption [13]; it has difficulty in revealing the nonlinear relationship between the along-track data and the grid data. This is unfortunate, as nonlinear processes are ubiquitous, particularly in mesoscale processes. A conspicuous example is that, when between two tracks, there exists an eddy, with a local extremum SSH (local high or local low) lying in between, then a linear interpolation scheme will never be able to reconstruct such a pattern—in fact, this is a benchmark that we will be examining in this study. Besides, OA, such as many other interpolation algorithms, is based on a given empirical model to calculate the interpolation field corresponding to the observation. Whether such an empirical model could really

approximate the mapping between observations and grid data are still a problem. Obviously, there is still much room for improvement for the satellite-derived SSH field reconstruction.

On the other hand, if we can find out a mapping that does not depend on the given model but, instead, depends on the available samples composed of the observations and the gridded ground truth, then the grid data between the tracks can be well reconstructed, provided that the new set of observations has the same format as the samples. This is the so-called “learning from samples” in machine learning [21]. Different from the traditional OA, which “learns from instruction,” this method does not rely on a model; it draws the needed functional relation from the training samples. In this regard, the methods of neural networks (NNs) [22] and NN-based deep learning [23], [24] have attracted enormous interest in recent decades. NNs are developed from the multilayer perceptron [25] and generally consist of three layers, namely, the input, output, and hidden layers. They do not depend on a particular model but work with linear or nonlinear transformations (called “activation function”) in hidden layers to convert inputs (from input layer) into outputs (to output layer) and adjust the structure of the NNs in order to minimize the error or loss function between outputs and the ground truth. Such examples include [26], who used an NN to interpolate SSH to a grid in a way of “pixel to pixel.” Their results are generally acceptable (the RMSE is about 4.7 cm), but, still, at some spots, the bias can exceed 10 cm.

In most of the current algorithms, all available data are put into an NN model for training. The adequacy is questionable, as the quality of data determines the effect of the NN model of concern. Indeed, it is a very important problem on how to determine the covariates for the outputs. Apart from this, while the “pixel-to-pixel” approach can allow one to map from the observations to each “pixel,” for 2-D or 3-D interpolation problems (such as SSH reconstruction), it may fail in dealing with the spatially distributed data. To address the first problem, in this study, we will use a newly rigorously developed causal inference tool (Liang–Kleeman information flow or IF for short; see Section II.A) to eliminate noncausal observations and hence achieve the data quality. For the second one, the principal component analysis (PCA), an efficient method for reducing the dimension of datasets, is used to extract the main spatial features of the data for NN. After these preprocessings, a multilayer NN (Section II.C) is to extract the mapping from the along-track SSH to the gridded SSH. For demonstration, we will focus on a region in the South China Sea where an eddy appears between two trajectories and traditional approaches fail. We first introduce the data in Section III and the IF-based NN in Section IV. The power of this new approach will be demonstrated using a benchmark problem (Section V). This study is summarized in Section VI.

II. METHODS

A. Information Flow

Since Liang and Kleeman [27], a series of studies have been conducted for a rigorous formalism of IF, which now has

been established from first principles in physics [28]. A causal inference technique is henceforth developed [29], validated, and applied with success in problems in different disciplines. A brief introduction of some material needed for this study is given in the following.

Consider, for an example, a 2-D stochastic dynamical system

$$dx = \mathbf{F}(x, t)dt + \mathbf{B}(x, t)d\mathbf{w} \quad (1)$$

where $\mathbf{F} = (F_1, F_2)$ is the deterministic components, $x = (x_1, x_2) \in \mathbb{R}^2$ is the state variables, $\mathbf{w} = (w_1, w_2)$ is a standard 2-D Wiener process, and $\mathbf{B} = (b_{ij})$ is the matrix of perturbation amplitude. Liang [30] showed that the transfer of Shannon entropy, or IF, from x_2 to x_1 is

$$T_{2 \rightarrow 1} = -E \left(\frac{1}{\rho_1} \frac{\partial F_1 \rho_1}{\partial x_1} \right) + \frac{1}{2} E \left(\frac{1}{\rho_1} \frac{\partial^2 g_{11} \rho_1}{\partial x_1^2} \right) \quad (2)$$

where $\rho(t; x_1, x_2)$ is the joint probability density function, $\rho_1(t; x_1) = \int_{\mathbb{R}} \rho dx_2$ is the marginal density of x_1 , $g_{11} = \sum_{k=1}^2 b_{1k}^2$, and E is the expectation with respect to ρ . The so-obtained IF, i.e., (2), has several nice properties, one being the “principle of nil causality” [28]: an event is not causal to another event if the evolution of the latter does not depend on the former. This is a principle that all other formalisms try to verify in applications, while in the above rigorous formalism, this is a proven theorem: if both F_1 (the deterministic component of the system) and g_{11} (the stochastic component) are independent of x_2 , then $T_{2 \rightarrow 1} = 0$. Moreover, Liang [31] proved that the so-obtained causality is **invariant upon any nonlinear coordinate transformation**, indicating that (2) is an intrinsic physical property, in contrast to those empirical formalisms.

The IF formula has been validated in many highly chaotic systems, such as baker transformation, Hénon map, Kaplan–Yorke map, Langevin equation, etc. [28], [32]. Under a linearity assumption, Liang [29] further established that it can be estimated from two time series, say, x_1 and x_2 , and the resulting maximum likelihood estimator is remarkably simple in form, involving only covariances between the time series

$$T_{2 \rightarrow 1} = \frac{C_{11}C_{12}C_{2,d1} - C_{12}^2C_{1,d1}}{C_{11}^2C_{22} - C_{11}C_{12}^2} \quad (3)$$

where C_{ij} is the covariance between x_i and x_j , $C_{i,dj}$ is the covariance between x_i and \dot{x}_j , and \dot{x}_j is the difference approximation of dx_j/dt using the Euler forward scheme. In terms of correlation coefficient, (3) becomes

$$T_{2 \rightarrow 1} = \frac{r}{1 - r^2} (r'_{2,d1} - r r'_{1,d1}) \quad (4)$$

where $r = C_{11}/(C_{11}C_{22})^{1/2}$ is the sample correlation coefficient between x_1 and x_2 and $r'_{i,dj} = C_{i,dj}/(C_{11}C_{22})^{1/2}$ is the “correlation coefficient” between x_i and \dot{x}_j . Obviously, two uncorrelated events ($r = 0$) must be noncausal ($T_{2 \rightarrow 1} = 0$); the converse, however, does not hold; that is to say, causation implies correlation, but correlation does not imply causation. In a simple mathematical equation, (4) fixes the long-standing debate over causation versus correlation in philosophy. So far as of today, the L-K IF has been widely applied in diverse

problems such as global warming [33], [34], El Niño and IOD [29], typhoon genesis prediction [35], space weather [36], chlorophyll variability [37], soil moisture versus precipitation [38], Finance [39], [40], and neuroscience [41], to name a few.

B. Objective Analysis

OA is an interpolation algorithm widely used in satellite remote sensing, which aims to estimate the value θ_x of a scalar variable θ at a point \mathbf{x} from measurements φ_r at a limited number of data points $\mathbf{x}_r = (r = 1, \dots, N)$ [12]. Here, θ is one realization out of a homogeneous statistical ensemble, which has a zero mean and some given covariance. Under this assumption, the least-square linear estimator for θ is

$$\hat{\theta}_x = \sum_{r=1}^N \left[C_{xr} \left(\sum_{s=1}^N A_{rs}^{-1} \left(\varphi_s - \frac{1}{N} \sum_{p=1}^N \varphi_p \right) \right) + \frac{1}{N} \varphi_r \right] \quad (5)$$

where

$$A_{rs} = \overline{\varphi_r \varphi_s} = F(\mathbf{x}_r - \mathbf{x}_s) + \mathfrak{E} \delta_{rs}$$

is the matrix of covariance between all pairs of observations, \mathfrak{E} is the variance of the errors, and δ_{rs} is the Dirichlet function. Here, we have used A_{rs}^{-1} to indicate the entries of A^{-1} , i.e., the inverse of A

$$C_{xr} = \overline{\theta_x \varphi_r} = F(\mathbf{x} - \mathbf{x}_r)$$

is the covariance between the quantity θ_x to be estimated and the r th measurement.

Equation (5) shows that such a calculation requires only the location of the data points and a knowledge of the covariance function $F = (\xi)$. Thus, for different realizations of the field θ_x , the estimate θ_x depends linearly on the observations φ_s . In other words, θ_x is a linear estimator.

C. Neural Network

The traditional methods of interpolating the along-track data to the grid data are mostly based on some empirical given models. These empirical models are often based on our understanding of the system. Compared to large-scale ocean processes, up to now, the understanding of mesoscale or submesoscale processes is still limited. It is therefore necessary to have a model-free method to map the data along the orbit and grid points. NN is one of the most popular model-free methods which are also widely used in marine science in recent years [42]–[45].

Unlike OA, the NN offers a way to do nonlinear transformations. In this study, a series of NNs are designed to realize the regression of the output label to the multidimensional inputs. Specifically, in one NN, there are n training samples, each sample containing an N -dimensional input variables and a one-dimensional output label. Then, the input and output of the i th ($i \in \mathbb{Z}[1, n]$) sample is $\mathbf{X}[i] = (x_{i1}, \dots, x_{iN})$ and $\mathbf{Y}[i] = y_i$, respectively. Fig. 2 shows the structure of the NN model. Input and output layers are connected by three fully connected hidden layers, consisting of 256, 64, and 16 neurons. After each fully connected layer, a nonlinear transformation and a

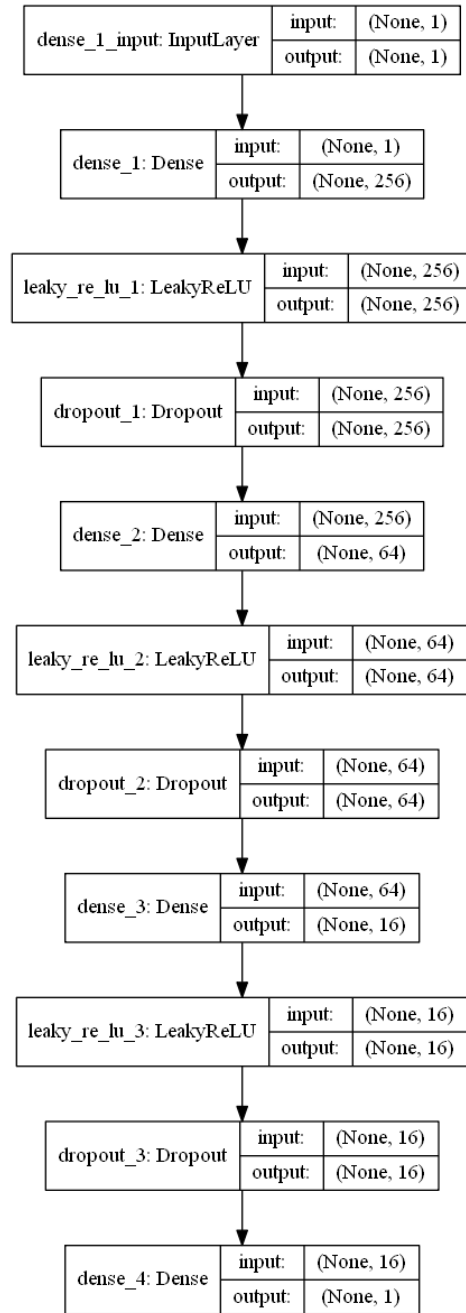


Fig. 2. Architecture diagram for the NN algorithm.

regularization are applied to accelerate the convergence. The former realized by an activation function enables the NN to learn the nonlinear relations between different layers. We use the leaky rectified linear unit (LeakyReLU [46]; parameter $\alpha = 0.2$) as the activation function. The regularization is a dropout method ([47]; parameter drop rates: 0.1). It works by randomly dismissing parts of the weight parameters, having the same effect as data augmentation [48]. For the NN, the loss function is chosen as the mean square error (MSE), and the optimizer is the adaptive moment estimation [49] (Adam,;parameter $lr = 0.0002$ and $\beta = 0.5$).

III. DATASETS

We use the Hybrid-Coordinate Ocean Model (HYCOM) dataset and the satellite altimetry of Jason-2 within the South China Sea region. HYCOM is a model with a hybrid coordinate in the vertical direction such that, in shallow waters, vertical grid points are geometrically constrained to remain at a fixed depth, while in deep oceans, an isopycnic coordinate is adopted [50]. This allows its simulation to be relatively accurate along the coast. In this study, we use the SSH derived from “HYCOM + NCODA Global 1/12° GOFs 3.1 41-layer Analysis (GLBy0.08 Experiment 9X.X).” It has a horizontal resolution of $0.08^\circ \times 0.08^\circ$ and a temporal resolution of 24 h (daily snapshot at 0 Z, start from January 1, 1994). The Jason-2 satellite altimetry data (including latitude, longitude, and date) [51] have a resolution of 1 s (1.0786 s) along the orbit and repeats at regular intervals in 10 days (9.9156 days, to be precise) (Fig. 1).

IV. INFORMATION FLOW-BASED NN

A. Preprocessing of Input Data

In order to minimize the error from the satellite altimetry data, this study assumes that the HYCOM data are the ground truth, and interpolates the HYCOM grid data onto the trajectory of Jason-2. Considering that the temporal sampling interval of Jason-2 (around 1 s) is much larger than the ground truth (once a day at UST 0:00) and the spatial sampling interval (about 0.137°) is of the same order as the ground truth ($0.08^\circ \times 0.08^\circ$), we do not interpolate the HYCOM grid data in time, but instead divide the ten-day (a period of Jason-2) orbital data into ten groups according to the day. More specifically, the sampling time of Jason-2 is rounded to integer days, and then, we put the same unit digit of sampling time into a group. For regional problem, the global trajectory data may be redundant [52], [53]. We hence discard the orbits far away from the South China Sea ($[100^\circ \text{ E} - 125^\circ \text{ E}$ and $0 - 24^\circ \text{ N}]$) and finally obtain ten sets of observations, each set containing a label (from 0 to 9) and the information of coordinates (longitude and latitude).

Since a time interval of 20 days (i.e., two periods) is commonly used as an e-fold time in OA [16], in this article, we also use this characteristic time to preprocess the along-track data. As shown in Algorithm 1, the along-track SSH used for interpolating the grid data at the date t_i (t is the time series with the unit of day) can be expressed as a label k (reflects the category of the track at t_i) and a 2-D array (one dimension is the input characteristics (latitude and longitude, t_i , SSH) and; the other one is made of the observations t_{i-20} to t_{i+19}).

B. Construction of the Model

In order to avoid the interference from the irrelevant data, the IF analysis is first applied. In Algorithm 2, its application eliminates the along-track observations that are noncausal to the principal components of the corresponding grid data. Considering the huge dimension of the grid data and the difficulty for the “pixel-to-pixel” model to learn the spatial

Algorithm 1 Data Preprocessing

Input: Grid data according to grouped latitudes and longitudes from the orbital data, time instants i for interpolation.

Step 1: Let $j = i - 20$. Interpolate linearly the j^{th} date of the grid data into the k^{th} group of the orbital data, save the interpolated data into the K^{th} cell, where

$$k = \text{mod}(j, 10),$$

$$K = \text{mod}(j, 10) + [\text{floor}(j/10) - (\text{floor}((i - 20)/10))] \times 10$$

with mod and floor being the remainder function and round-down function, respectively.

Step 2: If $j < i + 19$

$j = i + 1$ and go back to Step 1;

else

if $K > 39$

$j = 1$ and go to Step 3;

else

Output

end if

end if

Step 3: While $j < 5$

take the $(10j)^{\text{th}} - [(K - 39) + 10j]^{\text{th}}$ cell to the $[10j - 10]^{\text{th}} - [(K - 39) + 10j - 11]^{\text{th}}$

increment j

end while

Step 4: Reshape the data in cells into a vector $\mathbf{o}_{N_{\text{obs}}}$, where N_{obs} is the number of the orbital data.

Output $(\mathbf{o}_{N_{\text{obs}}})_i$ with a label $k (= \text{mod}(i, 10))$

Algorithm 2 IF-PCA-NN Training

Input: The grid data $\mathbf{G}_{N_G \times n}$, along-track data $\mathbf{O}_{N_{\text{obs}} \times n} = \{(\mathbf{o}_{N_{\text{obs}}})_i\}$ ($i = 1, \dots, n$), where N_G/N_{obs} is the grid/observation number and n the sample size

Step 1: Perform PCA for \mathbf{G} , get the matrix of the first M_G PCs $[\mathbf{P}\mathbf{C}_G]_{N_G \times M_1}$, where the variance of the M_G PCs is greater than or equal to 99% of the total variance, and the matrix of the time series coefficients of the M_G PCs $[\mathbf{A}\mathbf{G}]_{M_G \times n} = [(\mathbf{a}\mathbf{G})_g]_{M_1}$, where $(\mathbf{a}\mathbf{G})_g$ is the g^{th} PC's time series.

Step 2: Start with $g = 1$

Step 3: Using Eq. (3), calculate the Liang-Kleeman IF from the along-track data \mathbf{O} to the g^{th} grid data PC's time series $(\mathbf{a}\mathbf{G})_g$, perform significance test (at a 0.01 level), and select N_g along-track data $[\mathbf{O}_g]_{N_g \times n} (\in \mathbf{O}_{N_{\text{obs}} \times n})$ that are significantly causal, and their index ind_g

Step 4: Same as Step 1, but with along-track data \mathbf{O}_g . Obtain the matrix of the first $M_{o,g}$ PCs $[\mathbf{P}\mathbf{C}_{\mathbf{O}_g}]_{N_{\text{obs}} \times M_{o,g}}$, where the $M_{o,g}$ PCs contribute 99% of the total variance, and the matrix of the time series coefficients of the $M_{o,g}$ PCs $[\mathbf{A}_{\mathbf{O}_g}]_{M_{o,g} \times \hat{A}n}$, where $(\mathbf{A}_{\mathbf{O}_g})_{M_{o,g}}$ is the $M_{o,g}^{\text{th}}$ PC's time series of \mathbf{O}_g

Step 5: Put $[\mathbf{A}_{\mathbf{O}_g}]$ and $(\mathbf{a}\mathbf{G})_g$ into the neural network model in Section II.B, save the best network structure and weights $\mathbf{BNN}_g = \{bnn\}_g$

Step 6: If $g \leq M_g$ then

$g++$ (increment g)

return Step 3

else

Output

Output: PCs of the grid data $\mathbf{P}\mathbf{C}_G$, causal indices $\text{ind} = \{\text{ind}_g\}$ ($g = 1, \dots, M_1$), groups of the observation PCs $\mathbf{P}\mathbf{C}_O = \{\mathbf{P}\mathbf{C}_{\mathbf{O}_g}\}$ ($g = 1, \dots, M_1$) (where the $\mathbf{P}\mathbf{C}_{\mathbf{O}_g}$ is the PC matrix of the set consisting of the along-track data which are causal to the g^{th} PC's time series $(\mathbf{a}\mathbf{G})_g$ of the grid data \mathbf{G}) and of the grid data PCs $\mathbf{P}\mathbf{C}_G = \{\mathbf{P}\mathbf{C}_g\}$ ($g = 1, \dots, M_G$) and the neural network sets \mathbf{BNN}

structure from a global perspective, PCA [54] is used to simplify the problem from learning the mapping from the along-track data to grid data into mapping to the time series of the principal components (PCs) and hence greatly reduce the dimension of the NN model. Besides, PCA could also help to remove the impacts of extreme values on the whole datasets, and improve the generalization ability of the model [55]. This

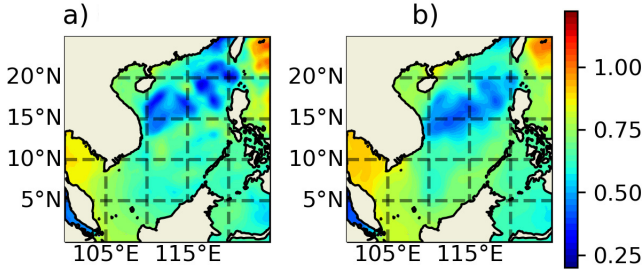


Fig. 3. SSH distribution in the South China Sea on March 26, 2020. (a) Ground truth. b) OA results.

is the IF and PCA-based NN (IF-PCA-NN). The workflow is summarized in the following algorithm.

Algorithm 2 provides the details of the IF-PCA-NN. When such a model is built with training samples, the SSH reconstruction now becomes easy. With the new along-track data coming in, we just need to use the output parameters to generate the desired grid data. The procedure is as follows. First, preprocess the input data using Algorithm 1. Second, use the causal indices *ind* to eliminate the noncausal observations. Third, perform PCA for the observations and obtain the time series of PC_O . Fourth, put the time coefficients of the causal observation PCs into the network sets and calculate the counterpart of the grid data. Finally, the grid data are reconstructed with the PC_G (PCs of grid data in the training set) and the corresponding time series $[\hat{A}_G]_{M_1 \times n_1}$ estimated with IF-PCA-NN.

V. RESULTS

A. OAed Map

As shown in Section II.B, the OA method only needs the locations of grid data and observation points, as well as the observed values. In Section IV.A, we assume that the HYCOM outputs as ground truth and construct the along-track data by the outputs. So \mathcal{E} is equal to 0 here. The covariance function is hence

$$C(dx, dt) = e^{-dx/a} e^{-dt^2/T^2}$$

where dx and dt are the spatial and temporal distance respectively, and the parameters $a = 110$ km and $T = 20$ day. The estimation of the gridded SSH is realized with (5).

Fig. 3 shows the HYCOM ground truth [Fig. 3(a)] and the OAed map [Fig. 3(b)] of SSH in the South China Sea on March 26, 2020. For the South China Sea, we take the whole along-track data in the region $[0-25^\circ \text{ N}, 98-130^\circ \text{ E}]$, which contains 12 792 observations in 40 days (from March 7 to April 15, 2020), with the OA method to map the grid data. From the ground truth, there are obvious low SSH zones between the area southwest of Luzon Strait and the region off Vietnam, and, particularly, four mesoscale cyclonic eddies with different sizes. The OA map has roughly captured the large feature, but only two eddies with limited amplitude are reconstructed. In particular, the strength of vortex off Vietnam is by far underestimated.

TABLE I
PERIODS COVERED BY THE TRAINING, VALIDATION,
AND TESTING DATASETS

Datasets	Beginning date	Ending date	Sample number
Training	01/01/1995	12/31/2016	8036
Validation	01/01/2017	12/31/2018	730
Testing	01/01/2019	12/31/2020	731

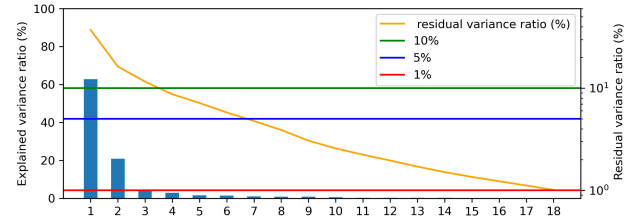


Fig. 4. Explained (bar, left ordinate) and residual (yellow line, right ordinate) variance ratios for the first 18 PCs of the grid data in the training set. The green, blue, and red lines denote the 10%, 5%, and 1% of the residual variance ratios (right axis), respectively.

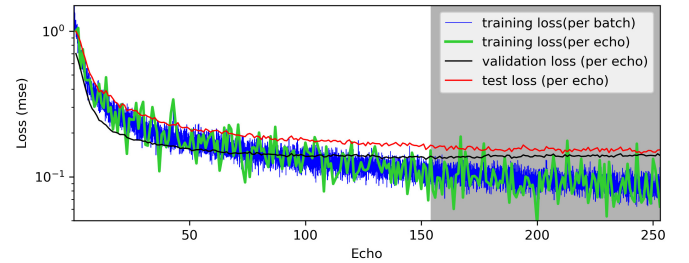


Fig. 5. Evolution of the loss functions for the first PC with different sets. The blue line indicates the training set (per batch), while the green, red, and black lines are for the training, validation, and testing sets, respectively (per echo).

B. Information Flow-Based NN

Region A $[15.28 - 20^\circ \text{ N}$ and $108 - 112.72^\circ \text{ E}]$ in Fig. 1 is the northern branch of the South China Sea where the west boundary current (SCSWBC) dominates. Just like the two famous boundary currents, namely Kuroshio and Gulf Stream, the SCSWBC is associated with a lot of mesoscale eddies, with significant seasonal variabilities (see [56]–[58]). This makes the SSH reconstruction for this region a big challenge.

For region A, we expand the interpolation region by 5° and call it the “observation region” (see the blue block in Fig. 1). For each sample if we are targeted to map at time step t_0 , there are 3812 along-track observations during t_{-19} to t_{20} . As shown in Table I, the samples are divided by date into training sets (8036 groups from January 1, 1995 to December 31, 2016), validation sets (730 groups from January 1, 2017 to December 31, 2018), and testing sets (731 groups from January 1, 2019 to December 31, 2020). Input these above sets into the model, and iterate until the validation loss reaches its minimum without updating through the next consecutive 100 iterations. Then, the model with the minimum validation loss is taken as the optimal one.

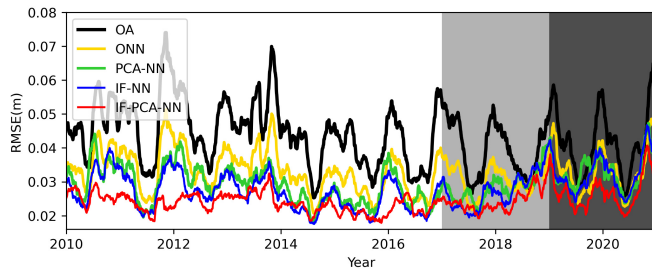


Fig. 6. Time series of the spatial average over region A of the RMSEs of SSH among the three experiments (unit: m; OA method, black line; ONN method, yellow line; PCA-NN method, green line; IF-NN method, blue line; and IF-PCA-NN, red line). Lightly shaded is the period over which the validation set is formed, and the period with dark shading is for test set.

In order to reduce the dimension of the model outputs, we first apply PCA to the grid data in the training set. As shown in Fig. 4, the eigenvectors of the first four PCs have been able to capture the basic features in region A (91.49% by variance). We choose the first 18 PCs, which makes 99% of the total variance. Next, Algorithm 2 is used to train the IF-PCA-NN model, and the mapping from the along-track data to the different PCs series is obtained successively. Take the first PC training process of IF-PCA-NN model as an example (Fig. 5). No matter which set it is with (training/verification/test set), the loss function generally decreases with iteration. The loss with the verification set does not reach a minimum (within the first 157 echoes) until the training is over 257 echoes. The deviations of the loss functions with the testing set and that of the verification set are roughly the same, implying that the samples of the training and verification sets have embedded all the variabilities in region A.

To illustrate the role of IF and PCA in the IF-PCA-NN model, we also design three NN-related experiments: PCA-NN, without IF (skip **Step 3** in Algorithm 2); IF-NN, without PCA (skip **Steps 1** and **4** in Algorithm 2); and ONN, original NN, without IF and PCA (skip **Steps 1, 3,** and **4** in Algorithm 2). Fig. 6 shows the time series of the spatial average of RMSE of the SSH among the five experiments (black—OA; yellow—ONN; green—PCA-NN; blue—IF-NN; and red—IF-PCA-NN). It can be seen that in the training set, the RMSEs of all four NN-related results are significantly smaller than that of the OA result (4.49 cm). Their RMSEs, from largest to smallest, are: 3.34 cm (ONN), 2.92 cm (PCA-NN), 2.65 cm (IF-NN), and 2.33 cm (IF-PCA-NN). For the validation set and the test set, the RMSE with the OA method is still around 4 cm (3.97 and 4.20 cm), which is consistent with the training set by a 99% F-test. For the NN-related models, their RMSEs increase slightly. For example, the best performed IF-PCA-NN increases to 2.44 (validation set) and 2.69 cm (test set). However, anyhow, these RMSEs are still significantly lower than that with the OA method.

To better show how the difference of the RMSEs with the five methods arises, we calculate the spatial distribution of the RMSE during the test set period (Fig. 7). Fig. 7(a) shows the standard deviation for the HYCOM ground truth [Fig. 7(a)]. It can be found that in the west of the region,

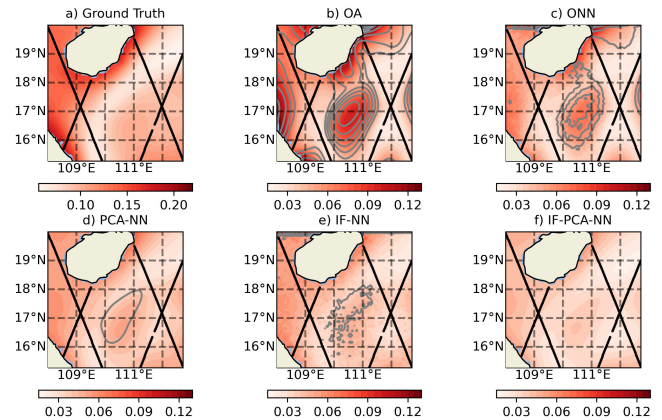


Fig. 7. Spatial distribution of the RMSE over test set (2019–2020). (a) Standard deviation of the HYCOM ground truth; the RMSEs (shaded, unit: m) and the normalization (>50% are marked by contour lines) of (b) OA; (c) ONN; (d) PCA-NN; (e) IF-NN, and; (f) IF-PCA-NN. The black lines mark the trajectory of Jason-2.

the along-track data are relatively sparse and the standard deviation of SSH is large. These account for the large RMSEs (shaded) in this region for the results with all the five methods [Fig. 7(b)–(f)]. Another observation is that there is a maximum region between the areas from Hainan Island to the offshore of Vietnam. It is located at gap of the Jason-2's orbits and hence makes sense. Compared to the OA result, the maxima on all the NN-related maps are significantly weaker. Clearly, NN-related models can effectively improve the problem caused by the gap. Among these NNs, the ONN has the maximum RMSE and obvious noise in distribution, while PCA-NN and IF-NN have their RMSEs significantly reduced in the gap area. Most notably, the IF-PCA-NN shows a very excellent performance, whose RMSE in the whole region can be further reduced.

In order to better understand the reason for the performance differences, we choose an eddy event occurring on March 26, 2020, for demonstration. As shown in Fig. 8, overall, the SSH has a pattern with an increasing trend overall from east to west. A conspicuous feature is an isolated cyclonic eddy southeast off Hainan Island. This eddy lies between the tracks (cf. Fig. 1) and hence poses a great challenge for interpolation. For this reason, the SSH reconstruction for region A makes an ideal testing example for our proposed algorithms.

Fig. 8(b)–(f) shows the reconstructed results with the five methods. They all can have the general trend reconstructed. However, when going to details, OA and ONN are far less accurate than the other three methods. For example, the OA and ONN reconstructions obviously underestimate the positive anomaly (especially OA) on the western side of Hainan Island. Moreover, as expected, OA fails to reveal the cyclonic eddy. By comparison, ONN performs slightly better; it captures the fragmentary low values, though with noise. The PCA-NN and IF-NN do capture the eddy, but the orientation and geometry of the eddy are not as those in Fig. 8(a). The pattern resulting from the IF-NN result is closer to the ground truth but is noisier than that from the PCA-NN. In contrast, the IF-PCA-NN method yields a rather appealing result, with

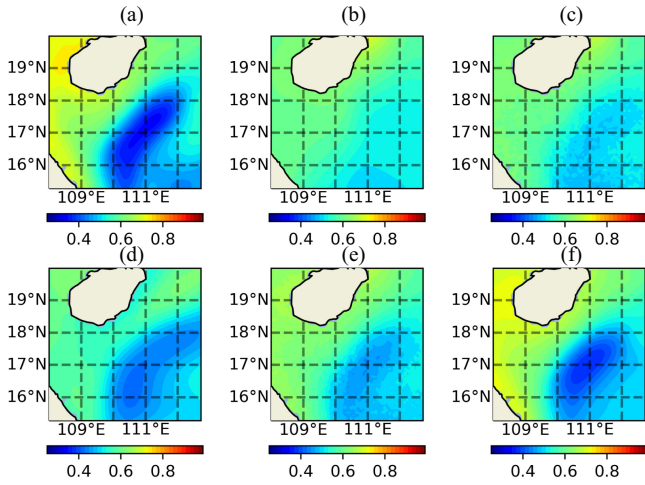


Fig. 8. Sea surface height (unit: m) for region A on March 26, 2020 where (a) is the HYCOM original field and (b)–(f) OA, ONN, PCA-NN, IF-NN, and IF-PCA-NN results, respectively.

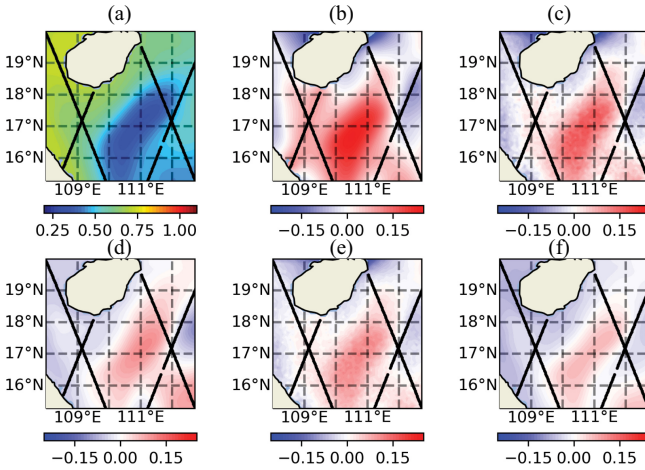


Fig. 9. Same as Fig. 8 but (b)–(f) are the deviations of the OA, ONN, PCA-NN, IF-NN, and IF-PCA-NN reconstructions from the ground truth. The black lines mark the trajectory of Jason-2.

the strength, size, shape, and orientation rather satisfactorily reconstructed. If compared quantitatively, the mean deviations and RMSEs with OA, ONN, PCA-NN, IF-NN, and IF-PCA-NN with the test set are, respectively, 1.69, -1.29 , 0.95, 0.79, and 0.72 cm, and 8.22, 6.88, 6.64, 5.13, and 2.50 cm. As the distribution of the deviation shown in Fig. 9, the isolated cyclonic eddy is exactly located within the gap of the Jason-2's orbits, where the maximum OA error results exist. As expected, OA cannot reconstruct mesoscale structure(s) lying in between the surrounding observations. In contrast, the deviations of the NN-related results within the gap, especially the causality-based NN (IF-NN and IF-PCA-NN), are much smaller.

Fig. 10 tracks the evolution of the eddy southeast off Hainan Island. It can be clearly seen that the eddy propagates from east to west and moves southward toward the area off Vietnam. This process is observed successively by different Jason-2 tracks within 20 days around March 26, 2020 (from March 16

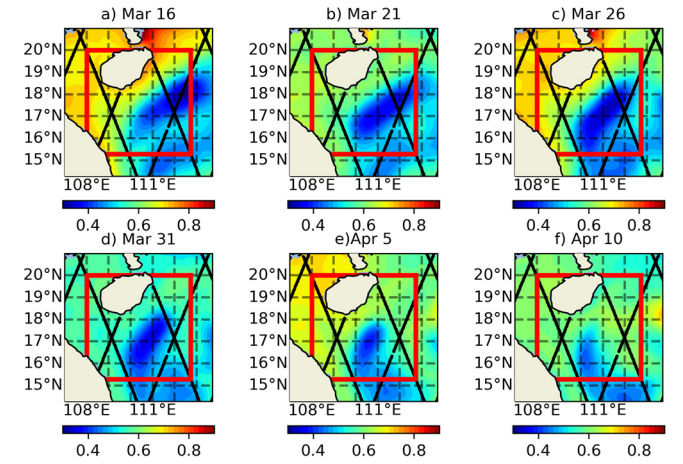


Fig. 10. Evolution of the eddy southeast off Hainan Island from March 16 to April 10, 2020.

to April 10, 2020). Although there are no observations in the area where the eddy appears on March 26, 2020, IF-PCA-NN can reconstruct the mapping from observations to the grid data by learning the intrinsic dynamic relationships between the observations at different times and thus reveal to us the eddy activity that would otherwise unobserved.

VI. CONCLUSION

The advent of satellite altimetry datasets of SSH has set a milestone in the advancement of oceanography and other Earth system sciences. However, while the along-track data coverage is dense, the relatively poor resolution between tracks poses a great challenge to the reconstruction of those processes such as mesoscale and submesoscale eddies. In this study, a machine learning algorithm has been developed to address this change, with an NN model combined with a causal inference technique based on the IF analysis [28], [29]. By discarding the redundant observations and reducing the dimension in the sample, the IF analysis and PCA are used respectively in order to construct a simple but nonlinear mapping from the along-track data to the grid data. It is shown that, with such an IF-based NN model, the characteristics of the grid data can be basically restored from the along-track data. As a demonstration, we picked an area in the South China Sea, where mesoscale and submesoscale eddies frequently appear but without satellite observations. By training the model as proposed above using the HYCOM data as ground truth, we immediately had the desired eddies reconstructed, which agree remarkably with the ground truth in strength, geometry, and orientation.

This study provides a new way of thinking for remote sensing data reconstruction. Traditional algorithms are based on a mapping method with some specific, preset model, while the NN method allows for the computer to find the intrinsic relationship between inputs (observations) and outputs (gridded data), so as to build mapping without relying on any model given *a priori*. By helping remove irrelevant factors, causal inference can speed up the process and improve the

performance of the NN to search for the best functional form for such a mapping. This technique to identify covariates is expected to play an important role in machine learning and artificial intelligence in the future.

It should be noted that the model training of the above method relies on 2-D gridded fields, while usually, we have only along-track data. Nonetheless, with the accumulation of more and more observational and modeling data, more accurate historical reanalysis grid data will be made available for the training purpose and, henceforth, the method is expected to show its power.

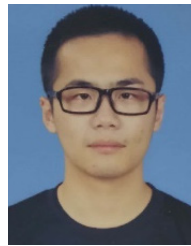
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